Comparison of stiff tension fracture test and notched beam level II fracture tests

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ABSTRACT: Using normal-strength concrete mixes, two methods for determining the cohesive traction versus crack opening displacement (σ -COD) relation of concrete are compared and contrasted. The first method, the "Stiff Tension Fracture Test" [Lenke & Gerstle 2001], uses a standard concrete cylinder, loaded in axial tension by a very stiff loading frame. The stiffness of the loading frame prevents snap-back and allows the tensile test to be conducted under open-loop load control in a standard universal testing machine. A shallow circumferential notch sawn into the surface of the cylinder at the central cross-section guides the crack formation. Three clip gages are employed to measure the crack opening displacement (COD), while the tensile load transferred across the crack plane is also monitored. An approximation of the complete normal traction versus crack opening displacement (σ -COD) relation is thus directly obtained. The second method, the "Level II (Closed Loop) Notched Beam Fracture Test", [Jenq & Shah 1985, Guinea, Planas & Elices 1994], uses a centrally notched beam in three-point bending. This test method is currently being considered by the American Concrete Institute Committee 446 as a test standard. This test uses feedback from the crack mouth opening displacement (CMOD) clip gage to control the rate of loading. An inverse method proposed by Planas and Elices is used to deduce, based upon the tensile strength and the recorded CMOD, load, and load point displacement, an assumed bilinear σ -COD relation. The σ -COD relations from the two test methods are compared. In addition, the statistical variability of the two methods is discussed.

1 INTRODUCTION

1.1 Background

Measurement of the fracture toughness of concrete has been a challenging problem for at least 40 years. Part of the problem has been lack of agreement about what type of model (linear elastic fracture mechanics model (LEFM), two-parameter fracture model, cohesive crack model, etc.) should be employed to represent fracture of concrete. The other part of the problem is in deciding what type of specimen and test method to use in the laboratory given the significant effect of concrete specimen size on the extracted fracture parameters [Bažant & Planas 1997].

Many laboratory fracture toughness tests have been suggested in the literature to determine fracture toughness of concrete as a quasi-brittle material [e.g. Evans and Marathe 1968, Jenq and Shah 1985, Hillerborg 1985, Karihalloo & Nallathambi 1989, Bažant & Kazemi 1990, Lenke & Gerstle 2001]. Many of these test methods were developed with a specific fracture model assumed a priori and therefore they yield inconsistent results and methods of fracture characterization of concrete. Furthermore, these tests aim to extract different fracture toughness features (e.g. fracture energy G_F, Mode I fracture toughness K_{IC}, critical crack opening displacement COD_{crit} and the brittleness length l_1). There is definitely a need for standardization of the fracture testing method to allow comparison between findings of different tests. The cohesive crack model appears to be gaining credibility as a reasonable fracture model for concrete. ACI Committee 446 has been considering standardizing two notched-beam tests - a Level I test (open-loop, to obtain only the initial linear part of the bilinear σ -COD curve) and a Level II test (closed-loop test, to obtain a bilinear approximation of the complete σ -COD curve) [ACI446 2009]. It appears that the fracture mechanics community generally agrees that a bilinear stress-COD curve is sufficiently simple, yet accurate, to represent fracture toughness of plain concrete.

Lenke and Gerstle [2001] developed and reported on a stiff tension fracture test (STFT) for obtaining the complete σ -COD curve. The repeatability of this test method appears to be good, as is evident from the test results presented by Lenke and Gerstle [2001] and also in this paper. On the other hand, there has been long history of determining the fracture toughness of concrete using the notched beam standardized tests. Experiments by Guinea et al. [1994] suggested the possible extraction of a bilinear σ -COD curve from the notched beam test. The four parameters defining the bilinear curve are dependent upon the tensile strength of concrete, Young's modulus, the load point displacement versus load relation, and the crack mouth opening displacement versus load relation obtained from the notched beam test. Comparisons between the fracture parameters extracted using both methods are not available in the literature. This paper evaluates the significance of difference between the fracture parameters extracted using both methods, including the fracture energies and the shapes of the stress-COD curves.

1.2 Scope of paper

In this paper, we seek to determine how the fracture parameters obtained using the STFT and the notched-beam Level II (denoted here as NB-LII) test compare. In Section 2, we present the concrete material. In Section 3, we present and discuss the test methods using the STFT test and the NB-LII test. In Section 4, we present the results of both tests on the same concrete mix (at somewhat different ages). In Section 5, we compare the results obtained from the two test methods and discuss the sources of difference. Conclusions are drawn in Section 6.

2 MATERIALS

The concrete used in both tests is normal plain concrete. The aggregate is 19 mm nominal maximum, limestone blend, dense graded. The water/cement ratio by weight is 0.54 (the mix contains 310 kg of normal type cement per cubic meter of concrete). No admixtures and no air-entraining admixture were used. The concrete has unconfined compression strength, f_c , of 33.7 MPa (4890 psi) at 56 days. The flexural strength (modulus of rupture) is 5.63 MPa (817 psi) at 56 days. The split tensile strength, f_{st} is 3.48 MPa (505 psi) at 56 days. The average Poisson's ratio is 0.19 at 56 days. The average Young's modulus is 32.6 GPa (4,658 ksi) at 56 days. Table 1 provides the basic characteristics of the concrete used in the fracture toughness tests.

Table 1. Density, compressive strength, split tensile strength and Young's modulus of concrete used in the fracture toughness tests.

Test #	Density	f (MPa)	f.	F
1050 //	(kg/m^3)		(MPa)	(GPa)
1	2365	34.6	3.21	31.0
2	2415	33.7	3.75	31.9
3	2410	33.7	3.75	31.9
4	2416	33.7	3.75	31.9
5	2416	33.7	3.75	31.9
6	2403	33.7	3.75	31.9
7	2411	33.7	3.75	31.9
8	2416	36.1	3.49	34.4
9	2420	36.1	3.49	34.4
10	2430	36.1	3.49	34.4
Mean	2410	34.5	3.62	32.6
Standard	±17.3	±1.1	±0.19	±1.3
deviation				

3 METHODS

3.1 Stiff Tensile Fracture Test (STFT)

The STFT is designed to test a standard 6" (15.24 cm) diameter by 12" (30.48 cm) long concrete cylinder. The STFT test is composed of two steel end caps into each of which is threaded a nominal 6" (15.24 cm) inside-diameter steel pipe jacket, into which the concrete specimen is subsequently epoxied. Three 1.25" (3.17 cm) diameter load rods (ASTM Grade B7 threaded rod) are bolted to both end caps in parallel with the specimen to provide the stiffness necessary to prevent snap back. The STFT loading frame is shown schematically in Figure 1.



Figure 1. Schematic of STFT [Lenke and Gerstle 2001].

The load rods are each instrumented with two 90° strain gage rosettes on opposite sides of the rods in a full bridge configuration with bending stress cancellation. Tensile load is applied via two concentric load rods threaded into the end caps. As the concrete begins to crack and ultimately separate, the instrumented load rods support progressively more of the applied tensile load, prevent-

ing snap back of the concrete. As load is applied, the nominal 1" (2.54 cm) gap between the upper and lower pipe jackets is monitored by clip gages. The gap increase between these jackets is approximately the crack opening displacement (COD) of the developing crack in the concrete.

As the tensile strength of the concrete is reached, the stress in the concrete reduces and the COD continues to increase reaching a critical crack opening displacement (COD_{crit}). By simultaneously loading the STFT device, monitoring COD, and monitoring the forces in the three steel stiffening rods, it is possible to extract an approximation of the stress-COD relation. The area under this relation is a measure of the fracture energy, G_F , of the specimen.

The STFT test was performed at 56 days of age while the NB-LII test was performed at 180 days of age. All testing specimens were cured in water tanks at 23 $^{\circ}$ C up to the day of testing. Figure 2 shows the STFT test apparatus. Analysis of the data was performed using the cohesive crack model [Hillerborg 1985] and the approach described in more detail by Lenke and Gerstle [2001].

3.2 NB-LII test

On the other hand, the notched beam Level II test can be performed to obtain a bilinear approximation of the complete stress-COD curve following the procedure presented in ACI 446 [2009], which follows the original work of Guinea et al. [1994]. In this test a beam is notched and is loaded in three-point bending as shown schematically in Figure 3. Feedback is provided using COD measurement to control the loading rate and to allow recording of the descending part of the load-displacement relation. ACI 446 [2009] provides a detailed description of the test specimen preparation, loading set-up and test procedure. A photograph of the beam test set-up is shown in Figure 4.



Figure 2. (a) STFT test setup used to extract cohesive crack model parameters. (b) Clip gauge measurements of crack opening displacement.



Figure 3. Schematic of NBL-II Test [ACI446 2009].

Three beams were tested using the NB-LII test. All beams were tested at 180 days of age. Analysis of the data was performed using the suggested method by ACI 446 [2009]. The initial compliance of the load-CMOD relationship C_i is determined as

$$C_{i} = \frac{\Delta(CMOD)}{\Delta P'} \quad . \tag{1}$$



Figure 4. Notched beam level II (NB-LII) test set-up to extract cohesive fracture parameters.

The initial compliance is then used to compute the elastic modulus of the concrete specimen as

$$E = \frac{6Sa_0}{C_1BD^2} V_1(\alpha'_0) \quad \text{with} \quad \alpha'_0 = \frac{a_0 + h}{D + h}, \qquad (2)$$

where E is the elastic modulus in GPa, S is the loaded span, C_i is the initial compliance in $\mu m N^{-1}$, B is the beam thickness in mm, D beam depth in mm, a_0 is the notch length, mm, h is the distance from the knife edges to the specimen surface, mm, and

$$V_{1}(\alpha) = 0.8 - 1.7\alpha + 2.4\alpha^{2} + \frac{0.66}{(1 - \alpha)^{2}} + \frac{4D}{S} \left(-0.04 - 0.58\alpha + 1.47\alpha^{2} - 2.04\alpha^{3} \right).$$
(3)

The residual load P_R is determined for CMOD = 2 mm or nearest point denoted w_{MR} . The load was corrected using Equation 4 and the far end tail constant was determined per ACI 446 [2009] as follows:

$$P_1 = P'_- P'_R$$
, (4)

where P' is the recorded load. The value of w_{MA} is determined as the intersection of the rising part of the corrected load P₁ versus CMOD curve with the CMOD axis. The far tail constant "A" is determined by least-square curve fitting of a quadratic relation of the load P₁ versus the quantity X derived from the points of record for which the corrected load is less than or equal to 5% of the corrected load peak. X is computed as

$$X = \left(\frac{4D}{S}\right)^{2} \left[\frac{1}{\left(w_{M} - w_{MA}\right)^{2}} - \frac{1}{\left(w_{MR} - w_{MA}\right)^{2}}\right].$$
 (5)

The effective peak load P_{max} is then computed as

$$P_{\max} = P_{\max} + \frac{A}{(w_{MR} - w_{MA})^2} , \qquad (6)$$

where P_{1max} is the corrected peak load. The plastic flexural strength of the beam is computed as

$$f_{p} = \frac{P_{max}S}{2Bb^{2}},$$
(7)

where B is the beam thickness and b is the ligament length equal to $D-a_0$ and S is the test span. The ratio of the tensile strength (determined from the splitting tension test) to the plastic flexure strength denoted x = f_t/f_p is used to compute the brittleness length l_1 as

$$l_1 = \kappa D \left[\frac{11.2}{\left(x^2 - 1\right)^2} + \frac{2.365}{x^2} \right] , \qquad (8)$$

where $\kappa = 1 - \alpha_0^{1.7}$ and $\alpha_0 = a_0/D$ is the notch-todepth-ratio. The brittleness length l_1 is used to determine the horizontal intercept of the softening curve w_1 as

$$w_{1} = 1000 \frac{2f_{t}}{E} I_{1}$$
(9)

The total work of fracture W_F is computed as

$$W_{\rm F} = W_{\rm Fm} + \frac{2A}{\delta_{\rm R} - \delta_{\rm A}} \tag{10}$$

where W_{Fm} is the measured work of fracture calculated as the area under the load versus the load-point displacement. A is the far end constant determined early, δ_R is the load-point displacement at the end of the test and δ_A is the load-point displacement at zero corrected load (P₁). The fracture energy G_F is then computed as

$$G_{\rm F} = \frac{1000 \,\,{\rm W}_{\rm F}}{\rm B \,\,b},\tag{11}$$

where B is the beam thickness in mm and b is the ligament length equal to $D-a_0$. The Mode I fracture toughness K_{IC} is extracted using the fracture energy,

 $G_{\text{F}},$ modulus of elasticity, E, and Poisson's ratio, $\nu,$ as

$$K_{IC} = \sqrt{\frac{E G_F}{(1 - \upsilon^2)}}.$$
(12)

The center of gravity of the softening curve w_G can be determined using the far tail constant A and the fracture energy G_F as

$$w_{G} = \frac{4A}{BSG_{F}} \times 10^{6}.$$
 (13)

The bilinear approximation of the softening curve is then determined using the mean value of the fracture energy G_F , the brittleness length l_1 and the horizontal intercept of the softening curve w_1 . The mean values denoted l_{1m} , G_{Fm} and w_{1m} are determined from the three fracture toughness testing specimens. The characteristic crack opening w_{ch} is determined as

$$w_{ch} = \frac{G_{Fm}}{f_t},$$
 (14)

where G_{Fm} and f_t are the mean fracture energy and the mean tensile strength respectively. The characteristic crack opening w_{ch} is used to determine the critical crack opening of the bilinear approximation curve w_c as

$$w_{c} = w_{ch} \frac{3w_{Gm} - w_{1m}}{2w_{ch} - w_{1m}} \times \left[1 + \sqrt{1 - \frac{2w_{1m}(3w_{Gm} - 2w_{ch})(2w_{ch} - w_{1m})}{w_{ch}(3w_{Gm} - w_{1m})^{2}}}\right]$$
(15)

The stress at the kink point of the bilinear approximation curve denoted σ_k is computed as

$$\sigma_{k} = f_{t} \frac{2w_{ch} - w_{lm}}{w_{c} - w_{lm}} \,.$$
(16)

The crack opening at the kink point of the bilinear approximation curve, w_k , corresponding to the stress σ_k is determined as

$$w_{k} = w_{1m} \frac{w_{c} - 2w_{ch}}{w_{c} - w_{1m}}$$
 (17)

Using the above procedure the bilinear approximation curve can be established using the three distinct points of the mean tensile strength f_t , the mean horizontal intercept of the softening curve w_{1m} and the kink point stress and crack opening σ_k and w_k respectively. The area under the linear approximation curve is equal to the mean fracture energy G_{Fm} . Verification proposed by ACI 446 [2009] to ensure the validity of the above analysis is to be performed.

3.3 Statistical analysis

The fracture toughness parameters extracted from both tests were statistically analyzed. The fact that the results of the STFT test were extracted from 10 specimens and results from the NB-LII test were extracted from 3 specimens precludes using just the mean values for comparison. We therefore performed the student t-test considering a two tailed distribution for unequal variance samples to compare between the two means. A 95% level of confidence was assumed sufficient to judge the significance of difference between the two means.

4 RESULTS

A typical stress-COD relation obtained from the STFT test is shown in Figure 5. A summary of the fracture parameters of the concrete extracted from the STFT test and NB-LII test are presented in Tables 2 and 3 respectively. A typical load versus CMOD relation obtained from the NB-LII test is shown in Figure 6. A typical load versus load-point displacement curve is shown in Figure 7. The bilinear approximation curve for the cohesive crack extracted from the NB-LII test is shown in Figure 8.



Figure 5. Typical stress-COD relationship obtained from the STFT test.

Table 2. Fracture toughness characteristics including COD_{crit} (μ m), fracture toughness K_{IC} (MPa m^{1/2}) and fracture energy G_r (N m/m²) extracted from the STFT test.

Specimen #	$COD_{1}(\mu m)$	$K_{\rm re}$ (MPa m ^{1/2})	$G_{\rm E}$ (N m/m ²)
1	/32	2.81	245
1	432	2.01	245
2	318	2.19	145
3	470	3.00	271
4	419	2.36	168
5	330	2.48	186
6	406	2.75	229
7	406	2.36	168
8	546	2.95	244
9	458	2.88	233
10	533	2.90	236
Mean	432	2.67	212.5
Standard	± 74.7	±0.3	±42.1
deviation			

Table 3. Fracture toughness characteristics including COD (μ m), Critical energy release rate K_{IC} (MPa. m) and fracture energy G_F (N.m/m²) extracted from the NB-LII test.

Specimen #	K_{IC} (MPa. m ^{1/2})	$G_{\rm F}$ (N. m/m ²)
	2.47	180.9
2	2.67	210.9
3	2.81	233.1
Mean	2.65	208.3
Standard	±0.17	±26.2
deviation		



Figure 6. Typical corrected load-CMOD relationship obtained from the NB-LII test.



Figure 7. Typical load versus load-point displacement of the NBL-II test.



Figure 8. Bilinear cohesive curve extracted using the NB-LII test results.



Figure 9. Comparison of the bilinear cohesive curve extracted using the NBL-II test and the STFT tests. The two curves were found to be similar.

5 DISCUSSION

Both tests (STFT and NB-LII) showed very similar behavior. Fracture energies, G_{Fm} , extracted from both tests have very close mean values 212.5 (±42.1) N. m/m² for the STFT test versus 208.3 (±26.2) N. m/m² for the NB-LII test. Statistical analysis using the student t-test showed the probability of being significantly different was about 16%. This is a low probability compared with a 95% level of confidence. Therefore it can be concluded that the two mean fracture energies extracted from the STFT test and the NB-LII test are not significantly different. We used the mean value of Young's modulus of elasticity extracted from the modulus of elasticity test to compute K_{IC} for both tests, therefore the K_{IC} from both tests were also not significantly different.

To extract the bilinear curve approximation for the NB-LII test, an estimate for the elastic modulus of the notched beam is computed using Equation (2). We note that the mean value for that elastic modulus was 44.7 (± 2.3) GPa which was found to be significantly different than the directly measured elastic modulus of elasticity 32.6 (± 1.3) GPa. While this difference did not result in changing the value for the fracture energy it affected the final shape of the bilinear curve. The difference in Young's modulus of elasticity might be attributed to the fact that the value extracted from the NB-LII test is based on a linear approximation of the initial slope extracted from the ascending part of the load displacement curve and therefore is prone to inaccuracy. It can also be attributed to the fact that all beams tested were of similar size; therefore, the extracted Young's modulus of elasticity and bilinear curve might be non-unique for incorporating a size effect. Further research is needed to examine that issue.

The cohesive curves extracted from both experiments were similar. This can be observed in Figure 9 where the two bilinear curves are compared. The NB-LII test showed a concrete critical crack opening displacement (COD_{crit}) of 511 mm. This value is derived from the three tests and is based on the approximation of the bilinear curve. This value is compared with the COD_{crit} of 432 mm computed as the average critical crack opening displacement from the 10 STFT tests. The COD_{crit} extracted from the NBL-II test was therefore 20% higher than that from the STFT tests. This can be explained by the fact that the COD_{crit} from the NB-LII test is an approximated value extracted from the average testing of the three specimens.

6 CONCLUSIONS

The fracture toughness parameters extracted from the stiff tension fracture test (STFT) were surprisingly similar to those extracted from the notched beam level II (NB-LII) test. The loading procedure and analysis suggested by ACI 446 [2009] for the NB-LII test were followed and produced a bilinear curve that is very similar to the cohesive bilinear curve extracted from the STFT test. The similarity of the results from the two different test methods is striking but could be coincidence. More testing is required to definitively determine whether or not the cohesive relations obtained from both test methods are indeed objective.

The uniqueness of the bilinear curve approximation extracted from the NB-LII test needs to be examined. There might be a need to consider multiple size specimens from the NB-LII test to extract a truly non-size dependent bilinear cohesive relation.

This scoping exercise has shown that both methods (STFT and NB-LII) tests appear to be meaningful tests that provide meaningful and very similar results. More testing is needed to verify this tentative conclusion.

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