ANALYSIS OF CRACK EVOLUTION IN CONCRETE THROUGH COMBINED ACOUSTIC EMISSION MONITORING AND MESOSCALE MODELLING

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Abstract: In this paper, the fracture process zone (FPZ) is investigated on unnotched and notched beams with different notch depths. Three-point bending tests have been realized on plain concrete under crack mouth opening displacement (CMOD) control. Crack growth is monitored by applying the acoustic emission (AE) technique. The comparison with a numerical model is also realized by using a mesoscopic approach. Such an approach is of particular interest in the analysis of interactions between the cementitious matrix and aggregates. Several AE parameters are examined during the entire loading process, and show that the relative notch depth influences the AE characteristics, the process of crack propagation, and the brittleness of concrete. The numerical load-CMOD curves show that the mesoscopic modelling reproduces well the notch effect and concrete failure. In order to improve our understanding of the FPZ, the width and length of the FPZ are followed based on the AE source locations maps in parallel with the numerical damage fields. An important energy dissipation is observed at the crack initiation in unnotched beams.

1 INTRODUCTION

Fracture of concrete is accompanied by the formation and evolution of an inelastic zone, referred to as the fracture process zone (FPZ), around the propagating crack tip. The existence of the FPZ is responsible of the nonlinear behaviour of concrete, and leads to complex phenomena like size effects. In fact, the length and the width of the FPZ are strongly influenced by the sizes of specimens/structures. Many researchers tried to characterize the FPZ and its evolution during crack extension in order to obtain size independent fracture parameters for the application of fracture
mechanics of concrete.

The objective of this paper is to characterize the FPZ and its evolution during the fracture process in unnotched and notched concrete beams with different notch depths based on the AE technique and finite elements calculations. The AE technique allows us a continuous real-time data acquisition, and thus the damage evolution during loading tests can be recorded. It is a passive method that has been proved to be very effective to locate microcracks and to study different failure modes in concrete structures [1, 2, 3, 4]. It presents a remarkable potential of applications, and has been used in the past to examine the influence of different parameters on the FPZ, such as the effect of aggregates [5, 6], porosity [7], creep [8, 9], notch depth [10], specimen geometry and type of loading [11]. The damage is then evaluated based on either statistical analysis of AE activity [12] or quantitative and signal-based techniques [4].

Several numerical models were capable to capture important characteristics that emerge in failure process and AE measurements [13, 14, 15]. A thorough investigation is here performed on this subject by modelling the behaviour of concrete at the mesoscopic scale. The mesoscale modelling presents many advantages in the understanding of the fracture process (i.e. the transition from diffuse damage to localized damage and final discrete failure) and the effect of concrete heterogeneities (size, volume fraction, shape of aggregates...) and mechanical characteristics of the components on macroscopic properties and the fracture behavior of concrete [16, 17, 18]. In particular, the multi-scales approach was found to be very useful to study the size effect on the strength of plain concrete structures [19, 20, 21]. In the present paper, the damage model used is the isotropic damage model developed by Fichant & al. [22], which is implemented in the finite element code Cast3m.

In section 2, experimental methods and damage model are presented. Then, fracture measurements are analysed, and the characterization of crack evolution at different loading stages is examined through AE technique and mesoscopic modelling. Finally, the effects of both the notch to depth ratio and size effect on fracture growth are described based on the experimental and numerical observations.

2 EXPERIMENTAL PROCEDURE

2.1 Materials and specimens

The experiments were realized by Grégoire & al. and reported in [23]. In the present work, the comparison between notched and unnotched beams is realized. The tests realized on notched beams were conducted on beams with depth of 200 mm, length of 700 mm, and effective span equal to 500 mm. Two notch to depth ratio values of 0.2 and 0.5 were considered and labeled SN200 and LN200, respectively. Tests realized on unnotched beams were conducted on beams with the same sizes as earlier (labeled UN200) and on beams with depth of 100 mm, length of 350 mm and effective span equal to 250 mm (labeled UN100). The thickness was kept constant for all the beams and equal to 50 mm.

Tests were conducted under closed-loop crack mouth opening displacement (CMOD) control. The CMOD measurement consists in recording the distance between two alumina plates glued on the bottom surface of the beam, on each side of the initial notch. For unnotched beams, the alumina plates were glued at a distance from midspan equal to half the depth of the beam because the location of the fracture process zone initiating from the surface was indeterminate (details may be found in [23]).

2.2 Acoustic emission technique

The AE system comprises an eight channel AEwin system, a general-purpose interface bus (PCI-DISP4) and a PC for data storage analysis. A 2D analysis with an AEwin algorithm is performed for the localization of AE events. In this study, 4 piezoelectric sensors with a frequency of 50-200 kHz and a resonance frequency of 150 kHz are used. The transducers are placed around the expected location of the FPZ to minimize errors in the AE event localization. They are placed on the specimens with silicon grease as the coupling agent. The
sensors form a rectangular grid location on one side of (75 x 120 mm²) for UN200 beams, (60 x 120 mm²) for UN100 beams, (105 x 120 mm²) for SN200 beams and (110 x 120 mm²) for LN200 beams [15].

The detected signals are amplified with a 40 dB gain differential amplifier. The recorded AE amplitudes range from 0 to 100 dB. In order to overcome the background noise, the signal detection threshold is set at a value of 35 dB slightly above the background noise. The acquisition system is calibrated before each test using a pencil lead break procedure HSU-NIELSEN [24]. Location accuracy is measured in the range of 5 mm by applying the pencil lead fracture at a known location of the specimen. The measured effective velocity is equal to 3800 m/s. Each waveform is digitized and stored, and signal descriptors such as rise time, absolute energy, duration, amplitude, average frequency and counts to peak are captured by AEwin system. The absolute energy is defined as the integral of the squared voltage signal divided by the reference resistance (10K-Ohm) over the duration of AE waveform. This feature is the true energy measure of the AE hit, and the unit is expressed in atto-joules (aJ).

3 DAMAGE MODEL

The chosen damage model is the isotropic model developed by Fichant et al. [22]. It allows to represent the unilateral effect due to crack closure effect (a decomposition of the stress tensor into a positive and negative part is introduced) and to obtain objective results independent of the length of the finite elements by controlling the fracture energy. This model is a simplified version of the micropor model [25], and is based on the relationship between the total stress and the effective stress $\bar{\sigma} (y)$ of the material:

$$\bar{\sigma} (y) = C^{-1}(y, \varepsilon (y)) : \sigma (y)$$

where $C^{-1}(y)$ is the initial stiffness of the material phases (the material is considered isotropic and linear elastic), $C^{-1}(y, \varepsilon (y))$ the stiffness of the damaged material, $\sigma (y)$ the local stress field in each point $y$ and $\varepsilon (y)$ the local strain field. For the isotropic version of the model, the expression linking the effective stress and the total stress is:

$$\bar{\sigma} = (1 - d) \sigma$$

where $d$ is the scalar value of the isotropic damage that only depends on the equivalent strain computed according to the elastic strain tensor $\varepsilon^e$:

$$\varepsilon_{eq} = \sqrt{\frac{\varepsilon^e : \varepsilon^e}{\varepsilon^e : \varepsilon^e}}$$

Damage increases when the equivalent strain $\varepsilon_{eq}$ is higher than the threshold strain $\varepsilon_{d0}$ with

$$\varepsilon_{d0} = \frac{f_t}{E}$$

where $E$ is the Young modulus and $f_t$ tensile strength. The evolution of the damage variable, due to external mechanical loads, has an exponential form:

$$d = 1 - \frac{\varepsilon_{d0}}{\varepsilon_{eq}} \exp \left[ B_t \left( \varepsilon_{d0} - \varepsilon_{eq} \right) \right]$$

where $B_t$ represents a damage parameter to control the slope of the strain softening constitutive relationships and is calculated as a function of the width $h$ of the finite element, and the fracture energy $G_f$.

$$\frac{G_f}{h} = \frac{f_t \varepsilon_{d0}}{2} + \frac{f_t}{B_t}$$

The Digital Concrete Model was developed with the aim to have a 'realistic' representation of cement-based materials by taking into account the random size distribution of heterogeneities [26]. A specific algorithm was developed to make a spatial and random distribution of these phases on the basis of a finite element grid. First of all, all grid elements have mortar properties. Then, aggregates are placed in the grid from the biggest to the smallest, according to the aggregate size distribution, such that no overlapping is obtained with other particles already placed. The properties of the grid elements located in
an aggregate area are those of aggregates. A regular grid is considered for the mesoscopic mesh with an 8 node quadrilateral finite element

3.1 Application on concrete at the mesoscale

The considered mesoscale for modelling the behaviour of concrete is the scale at which the material can be observed as a set of coarse aggregates embedded in a mortar matrix. Here, coarse aggregates are inclusions of size greater than 5 mm following the experimental aggregate size distribution, whereas mortar matrix is a mixture of finer aggregates and the cement paste (Table 1). The aggregates volume represents 30% of the total volume of concrete. The stability of results depending on the size of the specimen and the maximum diameter of the inclusion was performed in [26], and the criteria are taken into consideration here with specimen sizes equal to four times the highest inclusion diameter (L/Dmax>4) and finite element size equal to 0.8 time the smallest inclusion diameter. Note that the random aggregates distribution has a non-negligible effect on the stress concentration that can influence the cracking process and the path of the macro-crack [9].

Table 1: Aggregate size distribution of concrete

<table>
<thead>
<tr>
<th>φ (mm)</th>
<th>5</th>
<th>6</th>
<th>6.35</th>
<th>8</th>
<th>10</th>
</tr>
</thead>
<tbody>
<tr>
<td>Vf (%)</td>
<td>4.8</td>
<td>3</td>
<td>4.2</td>
<td>7.8</td>
<td>10.2</td>
</tr>
</tbody>
</table>

A regular mesoscopic mesh related to the middle part of concrete beams is generated, and two homogeneous concrete blocks are attached to the left and right end of the beam with progressively larger mesh to avoid stress concentration. The finite element meshes of concrete beams are presented in Figure 1. The loading is applied as an incremental vertical displacement of a rigid plate fixed at the top middle of the beam. The behavior of the plate is assumed linear elastic with a Young’s modulus ten times greater than that of concrete.

Figure 1: Meso-macro meshing and boundary conditions of concrete beams under three point-bending test

The numerical simulations are conducted under plane stress condition. The mechanical characteristics of aggregates are obtained from the literature: Young’s modulus of 60 GPa and tensile strength of 6 MPa are considered.

Numerical simulations are then performed to validate the choice of the mechanical properties defined for mortar and aggregates. For the homogeneous part, the parameters are determined by the mechanical concrete properties. The parameters used at the mesoscopic scale are summarized in Table 2.

Table 2: Model parameters for mortar and aggregates

<table>
<thead>
<tr>
<th></th>
<th>E</th>
<th>ν₀</th>
<th>fᵣ</th>
<th>Gᵣ</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(GPa)</td>
<td>(MPa)</td>
<td>(J/m²)</td>
<td></td>
</tr>
<tr>
<td>Mortar</td>
<td>26</td>
<td>0.2</td>
<td>3.8</td>
<td>60</td>
</tr>
<tr>
<td>Aggregate</td>
<td>60</td>
<td>0.2</td>
<td>6</td>
<td>80</td>
</tr>
</tbody>
</table>
4 STRUCTURAL RESPONSE ON THREE-POINT BENDING TEST

The influence of size and notch effect on the mechanical properties is investigated by comparing experimental and numerical load-CMOD curves. Calculations are performed with the digital concrete model for three mesh generations representing three different random aggregates distributions in the volume. The mesoscopic modelling reproduces well the experimental load-CMOD curves (Figure 2). Note that the nominal strength and the post-peak region of the load-displacement curves slightly vary with the random distribution of the aggregates. In addition, the results show a more important maximal stress for unnotched beams in comparison with the notched ones, with effects of both the notch depth and the specimen size.

![Figure 2: Comparison of numerical and experimental load versus CMOD curves for UN200, UN100, SN200 and LN200 beams.](image)

In order to have a better understanding of the notch and size effects, the three point bending tests have been monitored with the AE technique, and numerical simulations have been realized.

4.1 Effect of relative notch depth on AE characteristics and numerical damage evolution

Damage quantification is computed based on the AE activity represented by the cumulative number of AE hits (Figure 3a). The same processing is applied to the mesoscopic modelling by considering that each microcrack corresponds to a damaged Gauss point of the finite elements (i.e. when the damage parameter \( d \) is greater than 0). The cumulated number of damaged finite elements is plotted in Figure 3b. For the beams with depth of 200 mm, the results show that, as the notch depth decreases, the total number of AE hits increases requiring higher energy for overcoming interfacial bond along the ligament length.

For UN100, the rate of AE hits is similar to that for UN200 beams at the beginning, and reaches later values between the total number of AE hits for LN200 (presenting the same ligament length) and the total number of AE hits for UN200, which could be related to the additional energy required for the crack initiation in unnotched beams and to different crack lengths. The numerical damage evolution shows the same trend with most important damaged finite elements at the crack initiation site for unnotched beams and a total number of damaged finite elements proportional to the ligament length, and thus a good proportionality between the AE activity and the damage evolution observed through the numerical model. The cumulated AE energy and the strain energy released by finite elements follow the same trend, and give us information on initiation of cracks that progress up to failure, and thus can be related to the fracture energy measured on a global scale. Note that, even though the mesoscopic modelling can represent the stochastic properties of concrete, however the cumulative AE hits and damaged finite elements are only qualitatively comparable because the numerical concrete microstructure is not totally consistent with that of the original concrete.
4.2 AE damage localization and numerical damage fields

During the formation of a crack, energy is emitted as an elastic wave and propagates from the crack location to the AE transducers at the specimen surface. The localization map of AE events is based on arrival times of the first wave at each transducer and their respective velocity in the concrete specimen. Once the arrival time is picked, the least-square method is used to estimate the event location. The cumulative acoustic events are placed in 2D. The detected AE events of notched and unnotched beams are presented over a window covering the specimen height, with a width of 300 mm centered with respect to the notch (Figure 4). Each plotted point indicates a detected AE source.

In addition to the number of AE events, the parameters of the AE signal can provide valuable information on the fracture process. The initiation and propagation of cracks in concrete are generally correlated to AE signals amplitude. Extensive studies have shown that the absolute acoustic energy is also a significant parameter to characterize an event. Thus, the 2D localization maps of AE events are classified in terms of their levels of energy. Six energy levels are defined. It can be seen that AE events of higher energy levels are located in the core of the FPZ [9] outlining the crack path. The digital concrete model permits also to simulate the cracking process by following numerical damage fields. The crack opening is calculated with the numerical method suggested by Matallah et al. [27].

The localization maps of AE sources, the numerical damage localization and the crack opening are plotted at 50% of the maximum strength in the post-peak region (Figure 4). The crack opening images have been plotted on deformed beams to provide more visibility.

At the peak load, few AE events are detected, and damage begins to develop in a distributed manner. The localization maps show that the AE events appear first for LN200 beams, then for SN200, UN100 and UN200, respectively. The damage fields are localized in front of the notch at the mortar-aggregates interface. Once, they increase with loading to develop in the matrix, and localize in a single macro-crack.

At 50% in the post peak region, the localization maps also show different crack evolution with a more remarkable crack length for notched beams. The damage fields and crack opening obtained from the mesoscopic modelling also show different cracking evolutions. Cracks begin to join up together, and propagate in the mortar matrix exhibiting different realistic features as crack bridging and branching.

For unnotched beams, the localization of AE events begins earlier for UN100 than for UN200, with a more significant crack length, also indicating a more ductile behaviour for small beams due to different stress gradient along the ligament length. Further, a crack branching has been observed in the localization maps of UN200 and SN200 which could be due to an aggregate interlock, and indicating a rough and complex fracture surface along the ligament length of the beams.

During the terminal post peak region, the number of AE events continue to increase with
a lower rate due to the stable propagation of the crack. AE events are generated as a consequence of different toughening mechanisms through the crack faces on a micro and meso level, such as bridging and friction.

In order to improve our understanding of the FPZ, the width and length of the FPZ have been followed based on the AE source locations maps in parallel with the numerical investigation.

**SN200**

**UN200**

**LN200**

**UN100**

**Figure 4:** Localization maps of the AE events, numerical damage fields and crack openings at 50% of the maximal strength in the post-peak region for SN200 (A), LN200 (B), UN200 (C) and UN100 (D) beams.
4.3 Characterization of the FPZ

Different approaches were proposed to determine the length and width of the damaged zone using probability, statistic laws and different empirical relations [12].

In our study, the length of the FPZ is estimated based on AE events density along the ligament length. Figure 5(a) shows the density of AE events at each Y location, at the end of the rupture test for UN200, UN100, SN200 and LN200 beams. The crack propagates form the front boundary toward the back one induced by free surface. For notched beams, it can be seen that, ahead of the notch tip, the number of AE events progressively increases due to the front boundary, attains the maximum value (Nmax), then remains almost constant for some distance along the ligament length due to the steady state propagation of the crack, and decreases as the crack propagates towards the back boundary. The curves clearly follow the energy dissipation trend shown by the boundary effect model (which allow to model size effect on the specific fracture energy) and can be used to compute the real fracture energy. The dissipated energy during crack propagation from the front boundary to the back one can be taken into account by assuming a trilinear variation of the local fracture energy over the ligament length [29, 30]. However, for unnotched beams, the AE events density presents a remarkable peak near the front boundary indicating a more significant energy dissipation for crack initiation. Then it decreases along the ligament length.

The occurrence of AE events can be considered as a criterion to be adopted in order to follow the crack propagation through the beam depth for different loading levels. Therefore, the length of the FPZ can be defined as the length of the segment from the notch tip to the intersection of the histogram with the horizontal line located at 20% of Nmax. Fracture examination in concrete through combined techniques as digital image correlation and X-rays can give additional information. However, the monitoring of the evolution of the fracture length with AE technique shows similar trends as those above mentioned, and proved to be quantitatively acceptable [1, 31]. The relative fracture length, i.e. the ratio of fracture length from the crack mouth to the ligament length of the beam, obtained from the AE technique at different loading intervals, is plotted in Figure 5 (b) for UN200, UN100, SN200 and LN200 beams.

Fracture initiates earlier at 90% of the maximum strength in the pre-peak regime for the LN200 beams (followed by SN200), while the fracture growth of unnotched beams starts after the peak load. The relative fracture length in LN200 beam is more significant in comparison with those related to SN200, UN100 and UN200, and the relative fracture length of UN100 has values between those of UN200 and SN200 beams. The fracture growth is relatively abrupt at the beginning, and decreases at the end. A similar behaviour was also observed while studying size effect with a more remarkable crack length for smaller beams [31].

Figure 5: a) Cumulative AE events at each Y location at the end of the rupture test and b) evolution of relative crack length with load steps for UN200, UN100, SN200 and LN200 beams
The FPZ length was also computed using the mesoscopic approach by studying the evolution of the tangential stress $\sigma_{\theta\theta}$. This latter was numerically obtained along the crack path determined according to the post processing method developed by Matallah & al. [26]. Since the maximum value of the stress perpendicular to the crack path is obtained at the crack tip, the length of the FPZ was considered as the distance between the stress free crack tip ($\sigma_{\theta\theta} = 0$) and the crack tip ($\sigma_{\theta\theta} = f_i$) [32] (Figure 6). The results show that the crack appears at 40% and 50% of the maximum strength for notched beams with the mesoscopic modelling. However the same trends are observed as those related to the AE analysis with delayed cracks for unnotched beams at 90% and 100% of the maximum strength for UN100 and UN200, respectively. In fact, a large number of AE hits have been registered at the beginning with the AE technique without being localized due to the attenuation of emitted weak amplitude hits (for the source located in 2D, a wave must reach at least three sensors). In addition, the AE analysis does not give us precise information about the tip of the stress free crack because the criteria used for determining the length of the FPZ may cause a loss of information since we cannot exactly localize the crack tip position. All those elements may be responsible of the observed discrepancy.

Based on the localization maps, the width of the FPZ has also been estimated based on the horizontal line located at 20% of Nmax which separate the zone with a high number of events representing the localization of microcracking and the outside zone where the level of damage is lower [12] (Figure 7). The discrepancy between the widths of the FPZ is relatively important, and this could be due to different sources of error: the localization of AE events is realized in 2D on one face of the specimen. However, the crack path inside the thickness of the beams is different (in 3D) due to the internal heterogeneity of the material. In addition, the crack path is dominated by the distribution of aggregates and other softening mechanisms, and the width of the FPZ cannot correctly be determined when the main crack branches into microcracks in multiple directions. However, the results show that the width of FPZ tends to increase with the decrease of the relative notch depth. This behaviour was also observed in Otsuka and al. [1]

Those differences in length and width of the FPZ show a non-uniform stress distribution in the cross-sections of the beams with different sizes and different values of the relative notch depth which could be responsible, in combination with the softening behaviour of concrete, of the size effect in concrete structures.
6 CONCLUSION

An experimental and numerical study is presented in order to monitor fracture growth during three-point bending tests in notched and unnotched concrete beams. The mesoscale modelling reproduces well the notch effect on the load deflection curves of beams under bending. The total number of AE hits increases with the decrease of the relative notch depth, and shows a linear proportionality with the evolution of the damaged Gauss points obtained from the numerical model. The fracture process zone length has also been monitored with AE technique and the numerical model. The evolution of the fracture length is highly dependent on the relative notch depth due to the stress gradient. The initiation of the fracture is detected earlier in notched beams compared to unnotched beams with a higher relative crack length respectively. An additional energy dissipation for crack initiation has also been observed in unnotched beams. Additional studies are needed using a 3D mesoscopic modelling and a 3D localization algorithm for the AE analysis in order to evaluate the crack profile in 3D.

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8 REFERENCES


